

## Psychrometric and Energy Formulas Used For DOAS MRE Calculations

### To Calculate Dew Point & Mixing Ratio From Temperature, RH and Altitude

### SI Example

#### Inputs:

T= °C temperature  
 RH= % relative humidity  
 El= Elevation in meters (Not required for Dew Point)

#### Inputs

Temp= 32.2 °C  
 RH= 55.0 %  
 El= 198 m

#### Other Terms

Td= dew point temperature °C  
 w= mixing ratio in g/kg (multiply by 7 for grains/lb)  
 e= vapor pressure in mb (millibars)  
 es= saturated vapor pressure (mb)  
 Psta= station pressure (mb)

#### 1 Calculate The Saturated Vapor Pressure

$es = 6.11 \times 10^4 \cdot (7.5 \times T)^{(237.7 + T)}$  es= 47.95 mb  
<http://www.weather.gov/media/epz/wxcalc/vaporPressure.pdf>

#### 2 Calculate The Dew Point

$Td = (237.3 \cdot \ln(es \cdot RH/611)) / ((7.5 \cdot \ln(10)) - (\ln(es \cdot RH/611)))$  Td= 22.0 °F Td  
<http://www.weather.gov/media/epz/wxcalc/wetBulbTdFromRh.pdf>

#### 3 Calculate Mixing Ratio

##### 3.1 Calculate Vapor Pressure

$e = 6.11 \times 10^4 \cdot (7.5 \times Td)^{(237.3 + Td)}$  e= 26.4 mb

##### 3.2 Calculate Station Pressure

Three methods: 1) use pressure sensor on TR4601 sensor  
 2) Calculate based on temp and altitude  
 3) Calculate based on altitude

##### 3.2.1 Psta Using Temperature and Altitude (This will be used)

$Psta = Pb \times [(Tb / (Tb + Lb \times (h - hb)))^{(g0 \cdot MR)} / (R^* \times Lb)]$  Psta= 99100.5 Pa  
[https://en.wikipedia.org/wiki/Barometric\\_formula](https://en.wikipedia.org/wiki/Barometric_formula) Psta= 991.0 mb

Pb= Static Pressure at sea level (Pa) divide by 100 to convert Pa to mb  
 °C= Temp Celsius  
 Tb= Convert °C to °K  
 Lb= Temp Laps Rate (0-11000m)(K/m)  
 h= height above sea level (m)  
 hb= height a bottom of layer b (m)  
 R\*= universal gas constant  
 g0= gravitational acceleration (m/s<sup>2</sup>)  
 M= molar mass of Earths Air (kg/mol)

Pb= 101325  
 °C= 32.2  
 Tb= 305.35  
 Lb= -0.0065  
 h= 198  
 hb= 0  
 R\*= 8.3144598  
 g0= 9.80665  
 M= 0.0289644

##### 3.2.2 Psta Using Altitude

$Psta = 101325 \times (1 - 2.2577 \cdot 10^{-5} \times El)^{5.25588}$  Psta= 98968.9 Pa  
[http://www.engineeringtoolbox.com/air-altitude-pressure-d\\_462.htm](http://www.engineeringtoolbox.com/air-altitude-pressure-d_462.htm) Psta= 989.7 mb

##### 3.3 Calculate Mixing Ratio

$w = 621.97 \times (e / (psta - e))$  w= 17.01 g/kg  
<https://www.weather.gov/media/epz/wxcalc/mixingRatio.pdf> w= 119.0 gr/lb (IP)

Note pressure values are in mb  
 Multiply by 7 to get gr/lb

#### 4 Energy & Efficiency Values

##### 4.1 Calculating True Power (3 Phase)

$kW = (V \text{ (avg)} \times A \text{ (Avg)} \times PF \times 1.732) / 1000$  kW= 34.4 kW

Vave= Voltage: Measured once =( 469+469+470)/3 Vave= 469.0 volts (constant)  
 Aave= Amps: Measured in real time by minute example =(57.1+57.4+47.1)/3 Aave= 52.9 amps (used me)  
 PF= Power Factor: assumed to be 80% PF= 0.80% (constant)

##### 4.2 Calculate Dehumidifican Removal Efficiency (DRE)

$DRE = (cfm \times \text{delta grains} \times 0.0006429)$  DRE= 296.6 lbs/hr

cfm= Real time measured value cfm= 7410 measured  
 OA MR= Outdoor Mixing Ratio (gr/lb) real time measured/calculated value gr/lb= 118.8 measured/Ca  
 SA MR= Supply air Mixing Ratio (gr/lb) real time measured/calculated value gr/lb= 56.5 measured/Ca

##### 4.3 Calculating Moisture Removal Efficiency (MRE)

MRE= DRE/kW MRE= 8.6 lbs/kWh

**New Brunselft TX Location**

**Real Time Measured and Calculated Data**

Type	Abrev	SI Value	IP Values
<b>Measured Values</b>			
<b>OA Air Intake</b>			
Temp	Toa	<input type="text"/> °C	<input type="text"/> °F
RH	RHoa	<input type="text"/> %RH	<input type="text"/> % RH
Pressure	Poa	<input type="text"/> mb	<input type="text"/> in WC
<b>Supply Air 1</b>			
Temp	Tsa1	<input type="text"/> °C	<input type="text"/> °F
RH	RHsa1	<input type="text"/> %RH	<input type="text"/> % RH
Pressure	Psa1	<input type="text"/> mb	<input type="text"/> in WC
<b>Supply Air 2</b>			
Temp	Tsa2	<input type="text"/> °C	<input type="text"/> °F
RH	RHsa2	<input type="text"/> %RH	<input type="text"/> % RH
Pressure	Psa2	<input type="text"/> mb	<input type="text"/> in WC
<b>Amps</b>			
Line 1	A1	<input type="text"/> amps	
Line 2	A2	<input type="text"/> amps	
Line 3	A3	<input type="text"/> amps	
Average Amps	Aave	<input type="text"/> amps	
<b>Volts</b>			
Line 1	V1	469 VAC	
Line 2	V2	469 VAC	
Line 3	V3	470 VAC	
Average Amps	Vave	469 VAC	
<b>Power Factor</b>			
Power Factor	PF	80 %	
<b>AirFlow</b>			
Real time cfm	AF1	<input type="text"/> cfm	
Hourly cfm average	AF2	<input type="text"/> cfm	
<b>Altitude</b>			
Altitude above sea level	EI	198 m	650 ft
Type	Abrev	SI Value	IP Values
<b>Calculated Values</b>			
<b>Saturated Vapor Pressure (es)</b>			
OA Vapor Pressure	esoa	<input type="text"/> mb	
SA1 Vapor Pressure	ess1	<input type="text"/> mb	
SA2 Vapor Pressure	ess2	<input type="text"/> mb	
<b>Dew Point (Td)</b>			
OA Dew Point	OATd	<input type="text"/> °C Td	<input type="text"/> °F Td
SA1 Dew Point	SA1Td	<input type="text"/> °C Td	<input type="text"/> °F Td
SA2 Dew Point	SA2Td	<input type="text"/> °C Td	<input type="text"/> °F Td
<b>Saturated Vapor Pressure (e)</b>			
OA Saturated Vapor Pressure	O Ae	<input type="text"/> mb	
SA1 Saturated Vapor Pressure	SA1e	<input type="text"/> mb	
SA1 Saturated Vapor Pressure	SA2e	<input type="text"/> mb	
<b>Station Pressure (Psta) Calculation For Outside Air Usubg Temperature and A</b>			
Static Pressure at sea level (Pa)	Pb	101325 Pa	
°C Temp Converted to °K	Tb	<input type="text"/> °K	

Temp Laps Rate (0-11000m)(K/m)	Lb	-0.0065 K/m	
height above sea level (m)	El	198 m	
height a bottom of layer b (m)	hb	0 m	
universal gas constant	R	8.31446	
gravitational acceleration (m/s2)	g0	9.80665 m/s2	
molar mass of Earths Air (kg/mol)	M	0.028964 kg/mol	
Station Pressure	Pstat	<input type="text"/>	Pa
Station Pressure converted to mb	Pstat	<input type="text"/>	mb
<b>Calculate Mixing Ratio</b>			
OA Mixing Ratio	OAmr	<input type="text"/> g/kg	<input type="text"/> gr/lb
SA1 Mixing Ratio	SA1mr	<input type="text"/> g/kg	<input type="text"/> gr/lb
SA2 Mixing Ratio	SA2mr	<input type="text"/> g/kg	<input type="text"/> gr/lb
<b>Calculate True Power (3 Phase)</b>			
Total unit Kw consumption	kW	<input type="text"/> kW	
<b>Dehumidification Removal Efficiency (DRE)</b>			
OA - SA1 DRE	DRE1		<input type="text"/> lbs/hr
OA - SA2 DRE	DRE2		<input type="text"/> lbs/hr
OA - SA Average DRE	DREave		<input type="text"/> lbs/hr
<b>Moisture Removal Efficiency (MRE)</b>			
OA - SA1 MRE	MRE1		<input type="text"/> lbs/kWh
OA - SA2 MRE	MRE2		<input type="text"/> lbs/kWh
OA - SA Average MRE	MREave		<input type="text"/> lbs/kWh

Sample Strategy/Formula	
60 second sample rate 60 second sample rate 60 second sample rate	
60 second sample rate 60 second sample rate 60 second sample rate	
60 second sample rate 60 second sample rate 60 second sample rate	
60 second sample rate 60 second sample rate 60 second sample rate 60 second calculated	
Measurement at Start-up Measurement at Start-up Measurement at Start-up Calculated Constant Average	
Assumed value	
60 second sample rate real time 60 minute average	
Topographical Reference	
Sample Strategy/Formula	
=6.11X10 <sup>^((7.5xToa)/(237.7+Toa))</sup> SI =6.11X10 <sup>^((7.5xTsa1)/(237.7+Tsa1))</sup> SI =6.11X10 <sup>^((7.5xTsa2)/(237.7+Tsa2))</sup> SI	
= $(237.3 \cdot \ln(\text{esoa} \cdot \text{RH}/611)) / ((7.5 \cdot \ln(10)) - (\ln(\text{esoa} \cdot \text{RH}/611)))$ SI = $(237.3 \cdot \ln(\text{ess1} \cdot \text{RH}/611)) / ((7.5 \cdot \ln(10)) - (\ln(\text{ess1} \cdot \text{RH}/611)))$ SI = $(237.3 \cdot \ln(\text{ess2} \cdot \text{RH}/611)) / ((7.5 \cdot \ln(10)) - (\ln(\text{ess2} \cdot \text{RH}/611)))$ SI	
=6.11*10 <sup>^(7.5XOATd)/(237.3+OATd)</sup> =6.11*10 <sup>^(7.5XSA1Td)/(237.3+SA1Td)</sup> =6.11*10 <sup>^(7.5XSA2Td)/(237.3+SA2Td)</sup>	
<b>Altitude</b> Constant = Toa + 283.15 SI - Calculated every 60 sec	

Constant

See altitude

Constant

Constant

Constant

Constant

$= P_b \times \left[ \left( \frac{T_b}{T_b + L_b \times (h - h_b)} \right)^{\left( \frac{g_0 \times M}{R \times L_b} \right)} \right]$  SI every 60sec  
mb = Pa x 100 every 60 seconds

$= 621.97 \times \left( \frac{O_{Ae}}{P_{sta} - O_{Ae}} \right)$  SI X 7.0 for gr/lb  
 $= 621.97 \times \left( \frac{SA_{1e}}{P_{sta} - SA_{1e}} \right)$  SI X 7.0 for gr/lb  
 $= 621.97 \times \left( \frac{SA_{2e}}{P_{sta} - SA_{2e}} \right)$  SI X 7.0 for gr/lb

$(V_{avg} \times A_{avg} \times PF \times 1.732) / 1000$

$= (AF_2 \times (O_{Amr} - SA_{1mr}) \times 0.0006429)$  IP use gr/lb  
 $= (AF_2 \times (O_{Amr} - SA_{2mr}) \times 0.0006429)$  IP use gr/lb  
 $= (DRE_1 + DRE_2) / 2$

$= DRE_1 / kW$   
 $= DRE_2 / kW$   
 $= (MRE_1 + MRE_2) / 2$